

THE CASE FOR HYPERCRITICAL ACCRETION IN M33 X-7

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Received 2008 June 20; accepted 2008 September 26; published 2008 November 14

ABSTRACT

The spin parameter of the black hole in M33 X-7 has recently been measured to be $a_* = 0.77 \pm 0.05$. It has been proposed that the spin of the $15.65 M_\odot$ black hole is natal. We show that this is not a viable evolutionary path given the observed binary orbital period of 3.45 days since the explosion that would produce a black hole with the cited spin parameter and orbital period would disrupt the binary. Furthermore, we show that the system has to be evolved through the hypercritical mass transfer of $\sim 5 M_\odot$ from the secondary star to the black hole.

Subject headings: binaries: close — black hole physics — gamma rays: bursts — supernovae: general — X-rays: binaries

1. INTRODUCTION

The black hole spin in M33 X-7 has been very accurately measured to be

$$a_* = 0.77 \pm 0.05$$

in dimensionless spin parameter (Liu et al. 2008). The authors of this paper show that “In order to achieve a spin of $a_* = 0.77$ via disk accretion, an initially non-spinning black hole must accrete $4.9 M_\odot$ from its donor in becoming the $M_{\text{BH}} = 15.65 M_\odot$ that we observe today. However to transfer this much mass even in the case of Eddington limited accretion ($\dot{M} \sim 4 \times 10^{-8} M_\odot \text{ yr}^{-1}$) requires ~ 120 million years whereas the age of the system is only 2–3 million years. Thus the spin of M33 X-7 must be natal, which is the same conclusion that has been reached for two other stellar black holes” (Shafee et al. 2006; McClintock et al. 2006). However, Liu et al. (2008) noted that their spin derivation is model-dependent and subject to possible systematic errors.

Lee et al. (2002) predicted the spin parameters of Nova Sco (X-ray Nova Scorpii 1994) and Il Lupi (4U 1543–47) to be ~ 0.8 , with small effects after they were born in the explosion from mass accretion, i.e., predicted them as natal. However, Brown et al. (2007) showed that the rotational energy in such binaries scaled inversely with the donor mass at the time of common-envelope evolution preceding the explosion in which the black hole was born. The donor masses of Nova Sco and Il Lupi are $\sim 2 M_\odot$ whereas that of M33 X-7 was $\sim 80 M_\odot$, so Brown et al. (2007) suggested that the 3.45 day period of M33 X-7 resulted from a dark explosion; the high spin parameter would have resulted from mass accretion. This mass accretion would have had to take place at hypercritical rate as we discuss in this Letter.

We briefly comment on the hypercritical accretion for $\dot{M}/\dot{M}_{\text{Edd}} \sim 10^3$ or greater (Brown & Weingartner 1994). The scenario begins with Bondi accretion through the sonic point, which is often greatly larger than accretion at the Eddington limit. Because it had been worked out for a value of $0.31 \times 10^4 \dot{M}_{\text{Edd}}$ by Brown & Weingartner (1994) and because this

value is in the middle of those we shall use in stellar evolution, we use this value, although it could be much greater. The Brown & Weingartner (1994) work had been carried out earlier in all detail by Houck & Chevalier (1991) and checked by Chevalier (1995). We note that there is still considerable controversy in the astrophysical community about whether hypercritical accretion can take place or not. However, the general point we address is that if \dot{M} exceeds \dot{M}_{Edd} , then some of the accretion energy must be removed by means other than photons. In the case of hypercritical accretion, this excess energy can be carried off by neutrino pairs (Brown & Weingartner 1994). In the case of a neutron star, neutrino losses allow the matter flow to join smoothly onto the neutron star surface. In the case of a black hole, the neutrino losses let the matter flow smoothly over the event horizon and disappear into the black hole.

In the work of Podsiadlowski et al. (2003) we note two possible stages where hypercritical ($\dot{M}/\dot{M}_{\text{Edd}} \gtrsim 10^3$) or supercritical accretion may take place. Podsiadlowski et al. (2003) evolve a binary with $M_{\text{BH}} = 12 M_\odot$, $m_{\text{secondary}} = 25 M_\odot$, and an orbital period of 6.8 days.

1. Hypercritical accretion stage: They show that after the formation of the black hole, the secondary star will overflow its Roche Lobe and will transfer mass at a rate which peaks at $3 \times 10^{-3} M_\odot \text{ yr}^{-1}$. The binary detaches after about 10^4 years, once the secondary has been reduced to the mass of the black hole (or earlier if the stellar wind is strong enough).

2. Supercritical accretion stage: Mass transfer continues at a lower rate of $\sim 3 \times 10^{-6} M_\odot \text{ yr}^{-1}$ for up to another few 10^6 years through a directed wind.

Nevertheless Podsiadlowski et al. (2003) restrict accretion into the black hole to the Eddington limit. With this same assumption they were able to get GRS 1915+105 up to a spin parameter $a_* = 0.9$. However, McClintock et al. (2006) measured its spin parameter to be $a_* \sim 0.98$ – 0.99 . We were able to get the spin parameter up to the measured $a_* > 0.98$ with hypercritical accretion (Brown et al. 2007) (see the discussion on page 355 of Bethe et al. 2003).

If we suppress the assumption that the rate of accretion is

limited to the Eddington limit we observe that the binary Cyg X-1 in Podsiadlowski et al. (2003) would be able to transfer up to $\sim 30 M_\odot$ during the first thermal timescale (assuming there is that much mass in the system), and another few solar masses afterward, during the period where the black hole and the secondary star are detached, before the secondary fills again its Roche lobe during the red giant stage.

Cyg X-1, V4641 Sgr, and GRS 1915+105 are similar in that the donors in all cases were more massive than the black hole at the time the black hole was formed. The hypercritical accretion for GRS 1915+105 is necessary to bring a_* up to $a_* > 0.98$ (Brown et al. 2007). For the purposes of discussing Cyg X-1 including the hypercritical nature of the accretion the detailed evolution of Podsiadlowski et al. (2003) is useful. Given hypercritical accretion, M33 X-7 can be straightforwardly discussed in a similar way as we show in the next sections.

In § 2, we discuss what would be the consequences if the current spin of M33 X-7 were natal. We discuss a few problems in this scenario. In § 3 we discuss the case for hypercritical accretion in M33 X-7 as an alternative way of producing a high spin on the black hole in M33 X-7. We summarize our conclusions in § 4.

2. NATAL SPIN IN M33 X-7

In this section, we ask what the consequences would be for M33 X-7 were the currently observed spin of the black hole all natal.

Most important for the binary evolution is that the helium star (progenitor of the black hole) is spun up by the secondary star so that these “helium stars will be fully synchronized with their orbital motion throughout their core-helium burning”; i.e., there is tidal locking of the helium star with the secondary star (Van den Heuvel & Yoon 2007). Hence, the spin of helium star and the orbital motion of binary being locked together, and the angular momentum of the He star is transferred to that of the black hole as the helium star falls into the latter (Lee et al. 2002). In the evolution model of Lee et al. (2002) the natal spin parameter is almost entirely dependent on the preexplosion orbital period of the binary system. In that case, with the currently measured spin parameter $a_* = 0.77$, the preexplosion orbital period of M33 X-7 would be essentially the same as for Nova Sco, which Lee et al. (2002) predicted to be 0.4 days with spin parameter ~ 0.75 (see Fig. 12 of Lee et al. 2002). This prediction was confirmed by Shafee et al. (2006) with the measurement of $a_* = 0.65\text{--}0.75$ for Nova Sco.

Here we summarize a few problems with this scenario.

1. This tidal locking leads to a strange and complex situation for M33 X-7. Because of the short 0.4 day period, the helium star squashes inside the $\sim 70 M_\odot$ star, with orbital separation $a \sim 10 R_\odot$ (J. E. McClintock 2008, private communication). The tidal locking should be more effective in this case because these stars are much more massive and closer together than those considered by Van den Heuvel & Yoon (2007).

2. With high spin angular momentum of the helium star (black hole progenitor), the black hole is born in the Blaauw-Boersma explosion,¹ in which the black hole binary can have a system velocity due to the sudden mass loss during the explosion. With a given preexplosion orbital period of ~ 0.4 days and the present one of 3.45 days, M33 X-7 should have lost more than

half of the system mass and could not survive the explosion if there were no hypercritical accretion as we discuss below.

In the case of Nova Sco, the explosion involved a mass loss of several solar masses (Nelemans et al. 1999). The heliocentric radial system velocity of Nova Sco is $-150 \pm 19 \text{ km s}^{-1}$. After correction for peculiar motion of the sun and differential Galactic rotation, the magnitude of the velocity stands out as being higher than any other dynamically identified Galactic black hole candidate (Brandt et al. 1995). Given the donor mass of $\sim 2 M_\odot$ and the black hole mass of $5.1\text{--}5.7 M_\odot$, it lost nearly half of its system mass in the explosion (Nelemans et al. 1999). The reason why Nova Sco is the most energetic explosion among the soft X-ray transient sources is that the explosion energy has to be big enough to expel nearly half of its system mass. We believe that this energy was provided by the black hole spin. The present remaining rotational energy is 430 bethes (1 bethe = 10^{51} ergs). Lee et al. (2002) found that in Nova Sco most of the rotational energy is natal.

Given the same spin parameter in the natal spin of M33 X-7, it would have ~ 3 times more rotational energy than Nova Sco, because of the ~ 3 times more massive black hole, about half of $M_\odot c^2$! In between the explosion and the present time, no forces act on the binary assuming the (negligible) sub-Eddington rate of accretion. In other words, the explosion must convert the originally 0.4 day period into the present one of 3.45 days. We take the black hole mass after the explosion to be the present one, since accretion at the Eddington limit changes its mass negligibly in 2–3 million years.

In the Blaauw-Boersma explosion, assuming rapid circularization,

$$P_2 = \left(1 + \frac{\Delta M}{M_{\text{BH}} + m}\right)^2 P_1, \quad (1)$$

where the black hole mass $M_{\text{BH}} = M_{\text{He}} - \Delta M$ with the mass loss ΔM during the explosion, m is the mass of the secondary star at the time of the explosion, P_1 the preexplosion period, and P_2 is the postexplosion period. It is well known that once the mass loss is half of the system mass ($\Delta M_{\text{breakup}} = M_{\text{BH}} + m$) the binary becomes unstable and breaks up. This happens at

$$\left(\frac{P_{\text{breakup}}}{P_1}\right) = \left(1 + \frac{\Delta M_{\text{breakup}}}{M_{\text{BH}} + m}\right)^2 = 4. \quad (2)$$

With $P_1 \sim 0.4$ days for $a_* = 0.77$, the breakup period is 1.6 days, less than half the present 3.45 days observed in M33 X-7; i.e., the binary would break up during the explosion. Thus, there must be less mass loss in the explosion and mass must be transferred from the secondary star to the black hole following the explosion, as discussed by Bethe et al. (2003) in order to achieve the observed spin parameter.

From the above consideration, we believe that the present value of spin parameter $a_* = 0.77$ for M33 X-7 cannot be the natal one.

Nova Sco is completely different in the respect that the companion is $\sim 2 M_\odot$, much lighter than that in M33 X-7, and most of the black hole spin energy is natal. In Nova Sco, with the same natal period of $P_1 \approx 0.4$ days, the breakup period should be the same $P_{\text{breakup}} = 1.6$ days. The $\sim 2 M_\odot$ secondary star in Nova Sco is some billions of years old, so that even with accretion limited by Eddington, it could have transferred ap-

¹ For a detailed description of Blaauw-Boersma Kick, and a source of the relevant formula 1 see the Appendix in Brown et al. (2001).

preciable mass to the black hole. Lee et al. (2002) found this to be $0.41 M_\odot$ which, if conservative, would have increased the period of Nova Sco following the explosion to be 1.5 days. It is the proximity of this period to the 1.6 days (breakup period) which makes the system velocity of Nova Sco to be higher than any other Galactic black hole candidates.

3. EVOLUTION OF M33 X-7

In the previous section, we have discussed that the present value for the spin parameter cannot be the natal one. In addition, from Figure 12 of Lee et al. (2002) we see that the 3.45 day period corresponds to a low natal spin parameter $a_* \sim 0.12$ which is much lower than the observed one $a_* = 0.77$. So we believe that the spin-up of the black hole has to be caused by accretion from the companion. Knowing that the present-day orbital period and spin parameter of the black hole in M33 X-7, we can estimate from Figure 6 of Brown et al. (2000) that about 40%–50% of the mass of the black hole had to be accreted after its formation.

Now we can obtain the orbital period before the accretion in M33 X-7 assuming conservative mass transfer,

$$P_3 = \left(\frac{M_{\text{BH},4} \times m_4}{M_{\text{BH},3} \times m_3} \right)^3 P_4, \quad (3)$$

where subindex 3 indicates the recircularized values before the accretion starts and subindex 4 indicates the present values. Assuming that the black hole accreted $5 M_\odot$ from its companion after its formation, one can obtain

$$P_3 = \left(\frac{15.65 M_\odot \times 70 M_\odot}{10.65 M_\odot \times 75 M_\odot} \right)^3 3.45 \text{ days} = 8.9 \text{ days} \quad (4)$$

or a spin parameter of $a_* \sim 0.05$. This, of course, obligates us to reconstruct our calculation in equation (1); nevertheless, the preexplosion period is no longer restricted by the present-day spin parameter and the mass loss can be much smaller as we discuss below.

The black hole progenitor star had to be more massive than the secondary star in order for it to evolve into a black hole at least a few million years before the black hole formation and accrete hypercritically $\sim 5 M_\odot$ after the black hole formation so we could observe the present-day configuration of the system. Given such massive stars, we know that the mass loss through winds has to be considerable. So we know that the ZAMS mass of the black hole progenitor had to be larger than that of the secondary star, and that the ZAMS mass of the secondary star had to be larger than its mass anytime afterward, i.e.,

$$M_{\text{ZAMS}} > m_{\text{ZAMS}} > m_{\text{preexplosion}} \gtrsim m_{\text{after explosion}} \\ \gtrsim m_{\text{before accretion}} > m_{\text{after accretion}} + 5 M_\odot, \quad (5)$$

where M denotes the mass of black hole progenitor and m denotes the mass of the secondary star. We have assumed that the mass of the secondary only changes drastically when it fills its Roche lobe for the first time (the second time will occur when it becomes a red giant, but the amount of mass transfer is much smaller) after the explosion of the primary star as explained by Podsiadlowski et al. (2003): “After the brief turn-on phase, mass transfer occurs initially on the thermal timescale of the envelope reaching a peak mass-transfer rate of $\sim 4 \times$

$10^{-3} M_\odot \text{ yr}^{-1}$,” at which point it transfers hypercritically and in a conservative way, i.e., with little or no mass loss, $5 M_\odot$ to the black hole. This means the ZAMS mass of the black hole progenitor should be around $90 M_\odot$, and probably between 10 and $35 M_\odot$ right before the explosion, depending on the intensity of the winds (see Brown et al. 2001). This means that ΔM in equation (1) must be between 0 and $25 M_\odot$. So,

$$P_1 = \left(1 + \frac{\Delta M}{10.65 + 75} \right)^{-2} 8.9 \text{ days} \quad (6)$$

implies $5.3 \text{ days} \leq P_1 \leq 8.9 \text{ days}$, or a natal spin parameter in the 0.05–0.1 range for the black hole.

This result shows that the energy available for the Blandford-Znajek mechanism to produce an explosion is very small. Following Lee et al. (2000) the black hole spin energy which can be extracted is given as

$$E_{\text{BZ}} = 1.8 \times 10^{54} \epsilon_\Omega f(a_*) \left(\frac{M}{M_\odot} \right) \text{ ergs}, \quad (7)$$

where

$$f(a_*) = 1 - \sqrt{\frac{1}{2} (1 + \sqrt{1 - a_*^2})}. \quad (8)$$

Here $\epsilon_\Omega = \Omega_F / \Omega_H$ is the efficiency of extracting rotational energy which, for an optimal process, is ~ 0.5 , where Ω_F is the angular velocity of the magnetic field, and Ω_H the angular velocity of the black hole. We obtain “only” (as compared with the hundreds of bethes available in the Galactic transient sources; Brown et al. 2007) between 3 and 11 bethes of available energy.

This means that most likely the explosion was a dark one and the amount of expelled material was small if not zero, analogous to that proposed by Mirabel & Rodrigues (2003) for Cyg X-1.

4. CONCLUSIONS

In this Letter, we discussed a few problems were the currently observed spin of M33 X-7 all natal: first, the black hole progenitor overlaps with the companion star, and second, the binary will break up during the explosion in which the black hole was born.

We suggest that the hypercritical accretion has happened in M33 X-7 after the black hole formation which spins up the black hole after its formation. M33 X-7 is the ideal system to test hypercritical accretion on. Since $\dot{M}_{\text{Edd}} \equiv L_{\text{Edd}} / c^2 = 4 \times 10^{-8} M_\odot \text{ yr}^{-1}$ the necessary accretion to have the black hole torqued up by its companion requires ~ 120 million years to achieve the $5 M_\odot$ necessary to spin the black hole up to a spin of $a_* = 0.77$ (King & Kolb 1999) as we suggested. The age of the system is however only 2–3 million years (Orosz et al. 2007).

We think that hypercritical accretion was already established in Houck & Chevalier (1991), Brown & Weingartner (1994), and Chevalier (1995) by the disappearance of SN 1987A. However, it is good to have another proof as given by M33 X-7.

G. E. B. was supported by the US Department of Energy under grant DE-FG02-88ER40388. C. H. L. and I. H. P. were supported by Creative Research Initiatives (MEMS Space Telescope) of MEST/KOSEF.

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